A METHOD AND APPARATUS FOR MAKING
A CHANNEL ESTIMATE

BACKGROUND OF THE INVENTION

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1. Field of the Invention

The present invention relates to channel estimation in a telecommunication system, and more particularly, data-aided channel estimation.

10   ### 2. Description of Related Art

It is very well known that coherent methods of channel estimation give about 3 dB of gain over non-coherent methods, provided that perfect knowledge of the channel fading parameters (amplitude and phase) is known. In practical applications, such perfect knowledge is never achieved, and a receiver must

15   estimate the fading parameters. This estimation is prone to errors, and thus, the "promised" 3 dB gain may rapidly start to vanish as the accuracy of the channel-estimation algorithm decreases. This problem appears in communication systems where channel fading and coherent detection are present (e.g., CDMA2000, 3GPP, and ARIB - where the channel parameters are usually estimated from a

20   pilot signal). Common losses from channel estimation errors in these systems can range from 0.1 dB up to 3 dB, depending on the specifics of the channel and the system.

Under consideration is the problem of estimating the complex-valued channel gain (also called "complex fading coefficient") experienced by a BPSK-

25   modulated symbol transmitted over a single path of a (possibly multipath) fading

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channel. A complex discrete-time received sequence is generated by demodulation (e.g., correlator or matched filter) and sampling of each path. For symbol i, the effect of fading on the received signal, y_i, can be modeled as

$$y_i = a_i x_i + v_i$$

5 where a_i is the complex-valued fading coefficient, $x_i \in \{\pm 1\}$ is the transmitted data bit (which can be either +1 or –1), and v_i is the complex background additive white Gaussian noise with zero mean and per-component variance σ^2. It is assumed that the fading is sufficiently slow so that the cannel gain is approximately constant over consecutive symbols. Hence, the symbol subscript

10 on the channel gain a is removed.

Conventional DS-CDMA channel estimation is performed through the use of a reference signal known as a pilot. The pilot may be transmitted in a number of different ways. One approach is to provide a channel, separate from the data channel, exclusively for the pilot signal. This method is used by both the

15 European (UMTS) and the North American (CDMA 2000) third generation wireless systems. A second approach is to time-multiplex pilot symbols with data symbols. This approach is used, for example, in the Japanese third generation wireless system (ARIB). Although the above two methods have fundamental differences, the underlying concept is the same.

20 With pilot-aided (PA) channel estimation, the pilot data bit, χ_i, is known to the receiver. Without loss of generality, we assume that $\chi_i = 1$ for all pilot

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symbols. Therefore, for pilot symbol i, the received signal statistic $y_{i,p}$ is

$$y_{i,p} = a_p + v_i$$

5   where a_p is the complex channel gain for the pilot signal, v_i represents the

background noise and is Gaussian, and p represents that a variable is based on

pilot symbols. Typically, the transmit energy of the pilot signal is kept as small as

possible in an effort to minimize the consumption of battery power and added

interference. Hence, the pilot signal does not necessarily have the same energy

10 as the data signal. Since the goal is to estimate a and not a_p, the following

weighting is applied to the channel gain of the pilot signal

$$y_{i,p} = \beta a + v_i$$

15 where β is a known, chosen design parameter.

For each received pilot symbol, a simple individual estimated realization of

the channel gain, $\hat{a}_{i,p}$, can be formulated as

$$\hat{a}_{i,p} = y_{i,p}.$$

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Data-aided (DA) channel estimation offers an alternative approach by

making use of the data symbols in addition to (or in lieu of) the pilot symbols. The

difficulty with DA estimation is that the data symbols are not known *a priori* (as is

the case with pilot symbols), which makes the estimation more challenging – and

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more noisy too. DA channel estimation can be implemented in conjunction with PA channel estimation by means of a stage-by-stage iterative procedure. In the first stage, a PA-only channel estimate is generated. This estimate is then used to detect the data symbols, which in turn are used as new "pseudo-pilot" information

5   to revise the PA channel estimate. This process can be repeated, and may be implemented as a loop within the decoding stage of the receiver. Typically, the information in each data symbol is estimated, then the information is removed and a channel gain estimate is generated using an averaging window.

DA channel estimation is an efficient way to assist channel estimation

10   because it makes use of data information that is already available at the receiver. The goal is to reduce the pilot symbol overhead and/or reduce the required transmit energy of pilot symbols. However, conventional DA channel estimate methods are computationally intensive and exhibit larger than desired variance.

15   **SUMMARY OF THE INVENTION**

In the method of the present invention, estimated individual realizations of the complex-valued fading coefficient, commonly called channel estimates, are generated. According to the inventive method, these realizations are easy to generate and can produce a channel estimate that exhibits a smaller variance in

20   comparison to conventional methods.

A level of confidence for each possible value of a transmitted data symbol is determined based on a received data symbol corresponding to the transmitted data symbol. The confidence level associated with a particular possible value is

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the level of confidence that the transmitted symbol was the particular possible

value. Using the confidence levels, a channel estimate is generated.

Unlike conventional data-aided channel estimate methods, the method

according to the present invention does not require making an explicit calculation

5   (called a hard decision) of an estimate of the transmitted symbol. Instead the

present invention offers a soft decision alternative that does not require

performing any maximizations. Consequently, the methodology of the present

invention offers an easy means of determining a data-aided channel estimate that

exhibits a smaller variance in comparison to conventional methods.

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BRIEF DESCRIPTION OF THE DRAWINGS

The present invention will become more fully understood from the detailed

description given herein below and the accompanying drawings which are given

by way of illustration only, wherein like reference numerals designate

15   corresponding parts in the various drawings, and wherein:

Fig. 1 illustrates a plot of the confidence function $h(y_{i,d})$ versus the log-

likelihood ratio λ ;and

Fig. 2 illustrates an apparatus for making a channel estimate according to

one embodiment of the present invention.

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DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

In the method of the present invention, estimated individual realizations of

the complex-valued fading coefficient, commonly called channel estimates, are

generated. According to the inventive method, these realizations are easy to

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generate and can produce a channel estimate that exhibits a smaller variance in comparison to conventional methods.

Using the received signal $y_{i,d}$, the channel estimate is defined as:

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$$\hat{a}_{i,d} = h(y_{i,d})y_{i,d}.\qquad(1)$$

where $\hat{a}_{i,d}$ is the channel estimate, h() is any predefined function that can be designed based on a specific constellation and channel being used, i represents the ith estimate, and d represents that the parameter or variable

10   pertains to data symbols (as opposed to a pilot symbols).

For the purposes of discussion only, the method of the present invention will described for the bi-phase shift keying (BPSK) constellation and an over-the-air communication channel. In BPSK, the transmitted symbol is either +1 or –1. However, from the following disclosure, it will be understood that application of the

15   method of the present invention is not limited to a particular constellation or channel. In a preferred embodiment for BPSK modulation, $h(y_{i,d})$ is defined as:

$$h(y_{i,d}) = P(x_i = +1|y_{i,d}) - P(x_i = -1|y_{i,d}),\qquad(2)$$

20   where $P(x_i = +1|y_{i,d})$ is the *a posteriori* probability that a transmitted data symbol $x_i = +1$ was transmitted conditioned on the observation of the received data symbol $y_{i,d}$ corresponding to the transmitted data symbol x_i, and where $P(x_i = -1|y_{i,d})$ is the *a posteriori* probability that a transmitted data symbol $x_i = -1$ was transmitted conditioned on the observation of the received data symbol $y_{i,d}$

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corresponding to the transmitted data symbol x_i. Here, $P(x_i = +1 | y_{i,d})$ represents a confidence level, based on the received data symbol $y_{i,d}$, that the corresponding transmitted data symbol x_i had a value of +1. And, $P(x_i = -1 | y_{i,d})$ represents a confidence level, based on the received data symbol $y_{i,d}$, that the

5   corresponding transmitted data symbol x_i had a value of -1.

Using Bayes' rule, equation (2) can be rewritten as equation (3a) below:

$$P(x_i = +1 | y_{i,d}) = \frac{p(y_{i,d} | x_i = +1) P(x_i = +1)}{p(y_{i,d})} \qquad (3a)$$

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where $p(y_{i,d})$ represents a probability density function of the received statistic evaluated at $y_{i,d}$.

A similar expression exists for $P(x_i = -1 | y_{i,d})$.

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$$P(x_i = -1 | y_{i,d}) = \frac{p(y_{i,d} | x_i = -1) P(x_i = -1)}{p(y_{i,d})} \qquad (3b)$$

Under the assumption that $P(x_i = +1) = P(x_i = -1) = 0.5$ using the Law of

20   Total Probability, $p(y_{i,d})$ is given by equation (4) below:

$$p(y_{i,d}) = \frac{1}{2}(p(y_{i,d} | x_i = +1) + p(y_{i,d} | x_i = -1)) \qquad (4)$$

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The well-known log-likelihood ratio (LLR) is defined as:

$$\lambda(y) = \lambda_1(y) - \lambda_{-1}(y) = \ln\left(\frac{p(y|x=+1)}{p(y|x=-1)}\right) \qquad (5)$$

where ln() represents the natural logarithm. It is known that y conditioned on x is a complex Gaussian random variable with mean ax and per-components variance σ^2, (i.e., noise), where σ^2 is determined according to any well-known technique. Therefore, the LLR is given by equation (6) below:

$$\lambda(y) = \lambda_1(y) - \lambda_{-1}(y) = -\left(\frac{(y-a)^2}{2\sigma^2}\right) - \left(\frac{(y+a)^2}{2\sigma^2}\right) = \frac{2a^*y}{\sigma^2} \qquad (6)$$

Combining Equations (1) – (6) results in:

$$\hat{a}_{i,d} = \left(\frac{e^{\lambda(y_{i,d})}-1}{e^{\lambda(y_{i,d})}+1}\right)y_{i,d}. \qquad (7)$$

Returning to Equation (2), $h(y_{i,d})$ is given by:

$$h(y_{i,d}) = \frac{e^{\lambda(y_{i,d})}-1}{e^{\lambda(y_{i,d})}+1}. \qquad (8)$$

A plot of this function with respect to λ is given in Figure 1. The function is odd and is bounded by ± 1, and bears a strong resemblance to the sign() function.

As will be appreciated, h($y_{i,d}$) represents the confidence that the transmitted symbol x_i is a particular value in view of the corresponding received symbol $y_{i,d}$. Stated another way, h($y_{i,d}$) indicates the strength or degree of

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confidence that the transmitted symbol x_i is a particular value in view of the

corresponding received symbol $y_{l,d}$.

Next, the overall data-based estimate is found by averaging the individual

realizations of the channel estimate over a weighted time window:

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$$\hat{a}_d = \frac{1}{2N_d + 1} \sum_{j=l-N_d}^{l+N_d} K_{j,d} \hat{a}_{j,d} = \frac{1}{2N_d + 1} \sum_{j=l-N_d}^{l+N_d} K_{j,d} \left(\frac{e^{\lambda(y_{l,d})} - 1}{e^{\lambda(y_{l,d})} + 1} \right) y_{l,d} \qquad (9)$$

where $K_{j,d}$ is a weighting constant, $2N_d + 1$ is the window over which the

estimate is averaged, and N_d is a number of samples.

10   Unlike conventional data-aided channel estimate methods, the method

according to the present invention does not require making an explicit calculation

(called a hard decision) of an estimate of the transmitted symbol. Instead the

present invention offers a soft decision alternative that does not require

performing any maximizations. A simple evaluation of the LLR, a well-known

15   receiver calculation already made in most receivers, is used. Consequently, the

methodology of the present invention offers an easy means of determining a data-

aided channel estimate that exhibits a smaller variance in comparison to

conventional methods.

Once the appropriate pilot-aided (PA) and data-aided (DA) channel

20   estimates and their variances are obtained, they can be combined in an optimal

manner. In the present invention, optimality is defined as minimum variance in the

final estimate. The PA channel estimate $\hat{a}^{(p)}$ can be determined according to any

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well-known technique, and therefore will not be described. The variances σ_p^2 and

σ_d^2 of the PA and DA channel estimates $\hat{a}^{(p)}$ and $\hat{a}^{(d)}$ can be determined

according to any well-known statistical technique; and therefore will not be

described. The final channel estimate, $\hat{a}$ is a linear combination of the PA and

5   DA channel estimates,

$$\hat{a} = w_p \hat{a}^{(p)} + w_d \hat{a}^{(d)}, \qquad (10)$$

where w_p and w_d are non-negative constants. Assuming that $E[\hat{a}^{(p)}] = E[\hat{a}^{(d)}] = a$,

where $E[]$ represents the average value, the added constraint that

$$w_p + w_d = 1 \qquad (11)$$

10   ensures that $E[\hat{a}] = a$.

Under the assumption that the PA and DA channel estimates are

independent, the variance of the overall estimate is

$$Var(\hat{a}) = w_p^2 \sigma_p^2 + w_d^2 \sigma_d^2. \qquad (12)$$

To minimize this variance subject to the constraint in equation (11) and

15   w_p, w_d being non-negative, $w_d = 1 - w_p$ is substituted in Equation (12). Then,

equation (12) is differentiated with respect to w_p, set equal to zero, and solved for

w_p.   The result is

$$w_p = \frac{\sigma_d^2}{\sigma_p^2 + \sigma_d^2}, \qquad (13)$$

and

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$$w_d = \frac{\sigma_d^2}{\sigma_p^2 + \sigma_d^2} \qquad (14)$$

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A check of the second derivative confirms that the solution is indeed a minimum.

Accordingly, by substituting equations (13) and (14) into equation (10), the channel estimate can be calculated using the PA channel estimate, the variance of the PA channel estimate, the DA channel estimate and the variance of the DA channel estimate.

An apparatus for implementing the above-described embodiment of the present invention will now be described with reference to Fig.2. As will be appreciated from the forgoing, the apparatus of Fig. 2 forms a part of a receiver. Because the other components of the receiver are well-known, applicants have not illustrated and will not describe these other components for the sake of brevity.

As shown in Fig.2, a shift register 10 inputs the received symbols y_i from a demodulator (not shown). As alluded to above, also not shown are the well-known components for determining the per-component noise or variance σ^2, the pilot-aided channel estimate $\hat{a}_p$, the variance σ_p^2 of the pilot-aided channel estimate and the variance σ_d^2 of the data aided channel estimate. An LLR calculator 12 receives the received symbol y_i from the shift register 10 and the square of the standard deviation, and calculates the LLR of the received symbol y_i according to equation (6). As will be appreciated, equation (6) requires, during a first iteration, an initial channel estimate as an input variable. In a preferred embodiment, the channel estimate based on the pilot symbols is used as the initial channel estimate, and then each subsequent iteration uses the channel estimate determined based on the combined data aided and pilot-aided channel estimates as shown in Fig. 2.

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Next, a confidence factor generator 14 generates a confidence factor $h(y)$ according to equation (8) using the output of the LLR calculator 12. A multiplier 16 multiplies the confidence factor with the received symbol y_t on a per component basis to obtain an individual realization of the channel estimate based on the received data according to equation (1). A weighted time window averager 18 stores the output of the multiplier 16 and calculates a weighted average of the data-aided channel estimate according to equation (9).

A channel estimate combiner 20 receives the output of the weighted time window averager 18 and the pilot symbol based channel estimate, calculates the variances of the DA channel estimate and the PA channel estimate, and generates the channel estimate according to equations (10), (13) and (14). The channel estimate is then used in the conventional manner to determine the transmitted symbols x_t, and is also feedback to the LLR calculator 12 to be used in the LLR calculation.

The invention being thus described, it will be obvious that the same may be varied in many ways. Such variations are not to be regarded as a departure from the spirit and scope of the invention, and all such modifications are intended to be included within the scope of the following claims.